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# ARCHITECTURAL ACOUSTICS

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Topanga, California

***First Pan-American/Iberian Meeting on Acoustics***

Cancun, Mexico

2 – 6 December 2002

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# *Acoustics*

- Acoustics is the science of sound, including its production, transmission and effects - Allan D. Pierce, *Acoustics An Introduction to Its Physical Principles and Applications*, McGraw-Hill Book Company, New York, 1981 (ASA reprint 1989).

## *Architectural Acoustics*

- Sound in an Enclosure.  
(We all know what it is, but it's difficult to define.)

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**Density:**  $\rho_o(P_o, T)$

**Pressure:**  $P_o \approx 100 \text{ kPa}$

$p(t)$  = instantaneous

$p$  = effective =  $\sqrt{\langle p^2(t) \rangle}$

**Frequency/ Wavelength:**

Speed of Sound:  $c = \lambda f$

$$c = 331.4 \sqrt{\frac{T}{273}}$$

$$c = \gamma \frac{P_o}{\rho_o}$$

# Log Notation

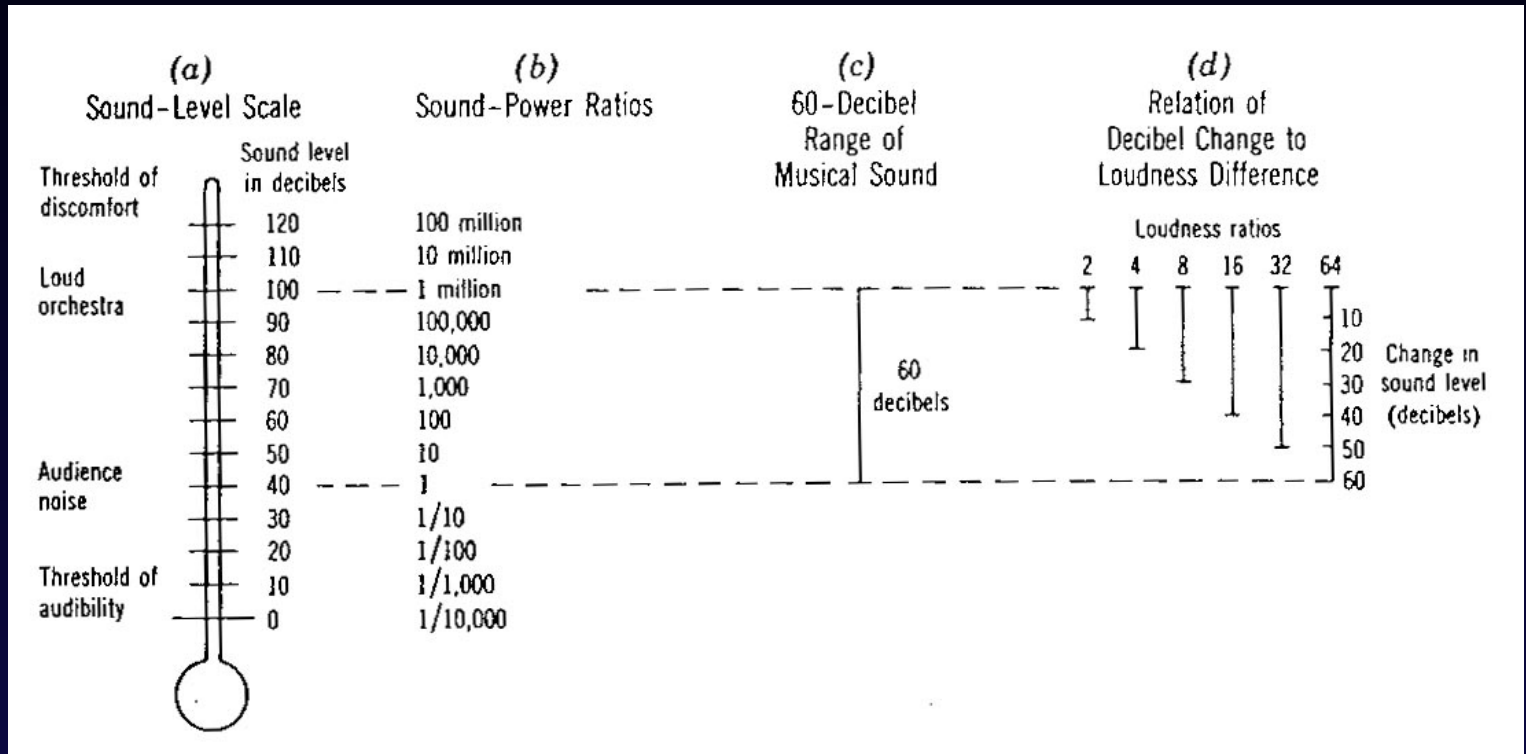


Figure 1

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# *SPL (sound pressure level)*

$$L_p = \text{SPL} = 20 \log p / p_{\text{ref}}$$

$$p_{\text{ref}} = 0.00002 \text{ Pa}$$

$$\text{Pa} = [\text{N}/\text{m}^2] = [\text{Kg}\cdot\text{m}/\text{s}^2\cdot\text{m}^2] = [\text{kg}/\text{s}^2\cdot\text{m}]$$

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# *SWL (sound power level)*

$$SWL = 10 \log W / W_{ref}$$

$$W_{ref} = 1 \times 10^{-12} \text{ W} = 1 \text{ pW}$$

$$W = [\text{kg} \cdot \text{m}^2 / \text{s}^3]$$

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# *I (intensity)*

$$L_I = IL = 10 \log I / I_{\text{ref}}$$

$$I_{\text{ref}} = 10^{-12} \text{ W/m}^2 = 1 \times 10^{-12} \text{ kg/s}^3$$

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# Waves

PLANE:

$$\frac{\partial^2 p}{\partial x^2} = \frac{1}{c^2} \frac{\partial^2 p}{\partial t^2}$$

COMPLEX  
FORM OF THE  
HARMONIC  
SOLUTION



$$P = A e^{j(\omega t - kx)} + B e^{j(\omega t + kx)}$$



# Waves

CYLINDRICAL:  $\nabla^2 p + k^2 p = 0$  ( $k = T/c$ )

$$\nabla^2 = \frac{1}{w} \frac{\partial}{\partial w} \left( w \frac{\partial}{\partial w} \right) + \frac{1}{w^2} \frac{\partial^2}{\partial \phi^2} + \frac{\partial^2}{\partial z^2}$$

One solution:

$$p = A \left[ J_0 \left( \frac{2\pi v w}{c} \right) + i N_0 \left( \frac{2\pi v w}{c} \right) \right] e^{-2\pi i v t}$$

$\rightarrow$   
 $W \rightarrow \infty$   $A \sqrt{\frac{2}{\pi k w}} e^{i k (w - ct) - i(\pi/4)}$

$$k = \frac{2\pi v}{c} = \frac{2\pi}{\lambda}$$

$\rightarrow$   
 $W \rightarrow 0$   $i \frac{2A}{\pi} \ln(w) e^{-2\pi i v t}$

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# Waves

SPHERICAL:

$$\frac{1}{r^2} \frac{\partial}{\partial r} \left( r^2 \frac{\partial p}{\partial r} \right) = \frac{1}{c^2} \frac{\partial^2 p}{\partial t^2}$$

if  $a \ll \lambda$  then  $p/r \gg \partial p / \partial r$  @  $r = a$

$$P \cong \frac{\rho}{4\pi} \frac{dS}{dt} \quad \text{at } r = a$$

$$p \cong \frac{\rho}{4\pi r} S' \left( t - \frac{r}{c} \right) \quad \text{where } S'(z) = (d/dz)S(z)$$

$S = \text{Total Flow}$

# Human Factors

RANGE  
OF  
AUDIBILITY:

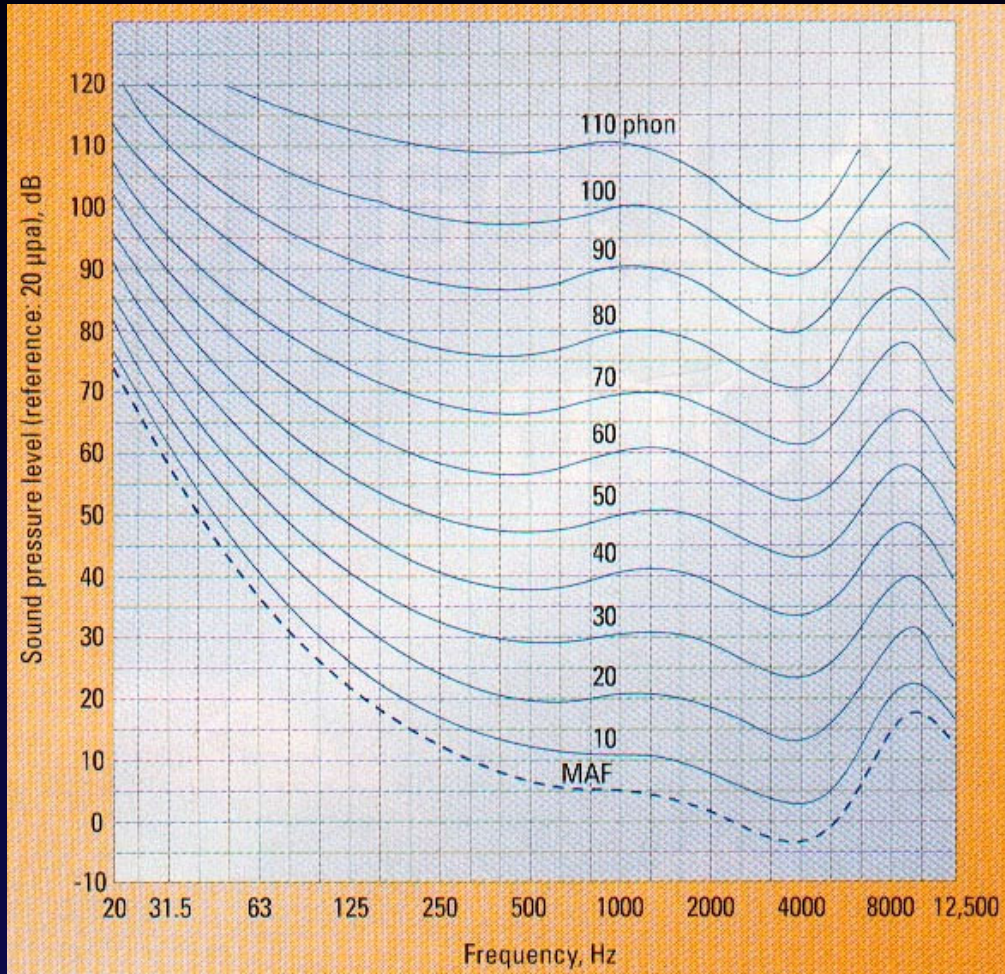


Figure 2

# Human Factors

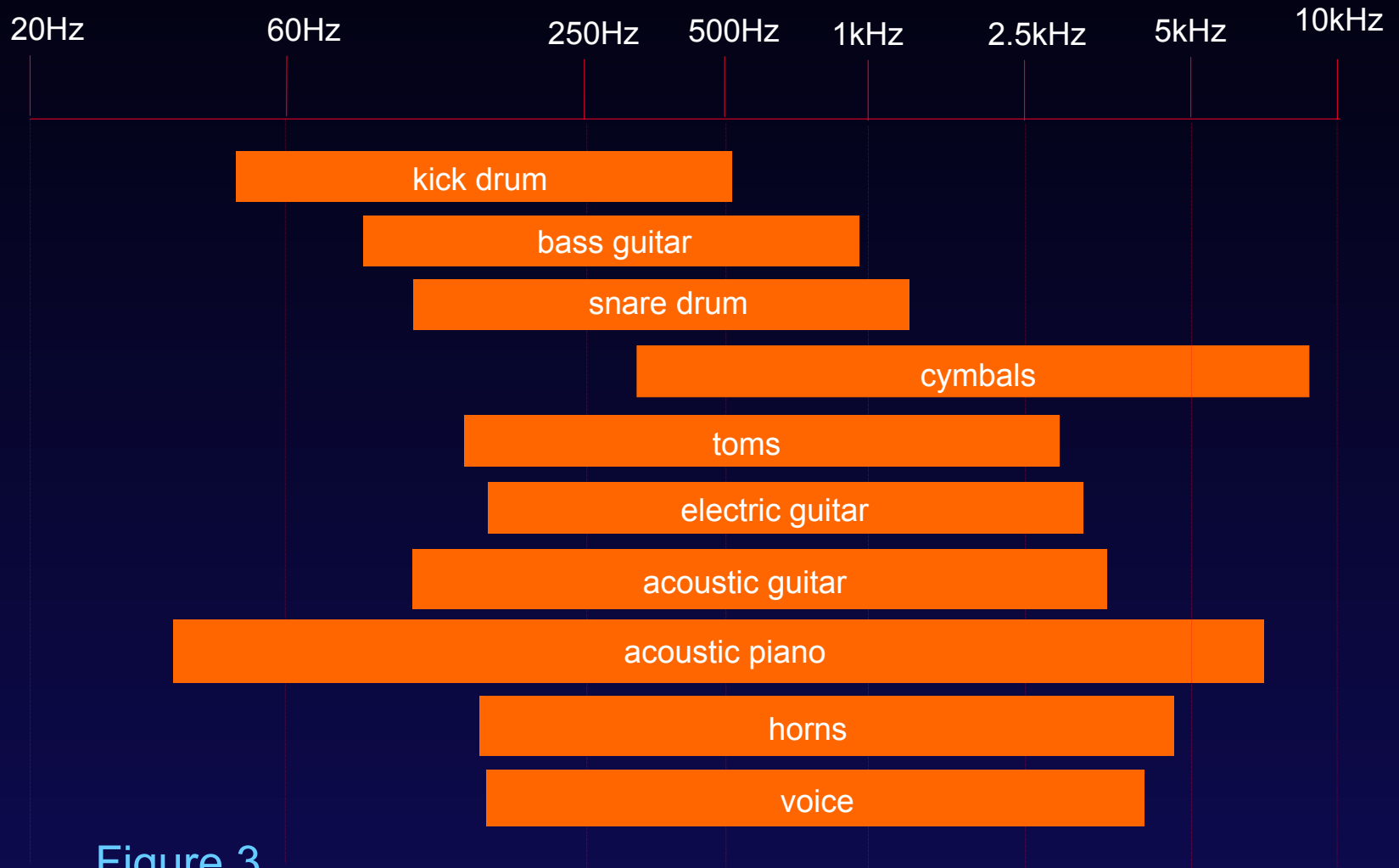


Figure 3

# Human Factors

Range

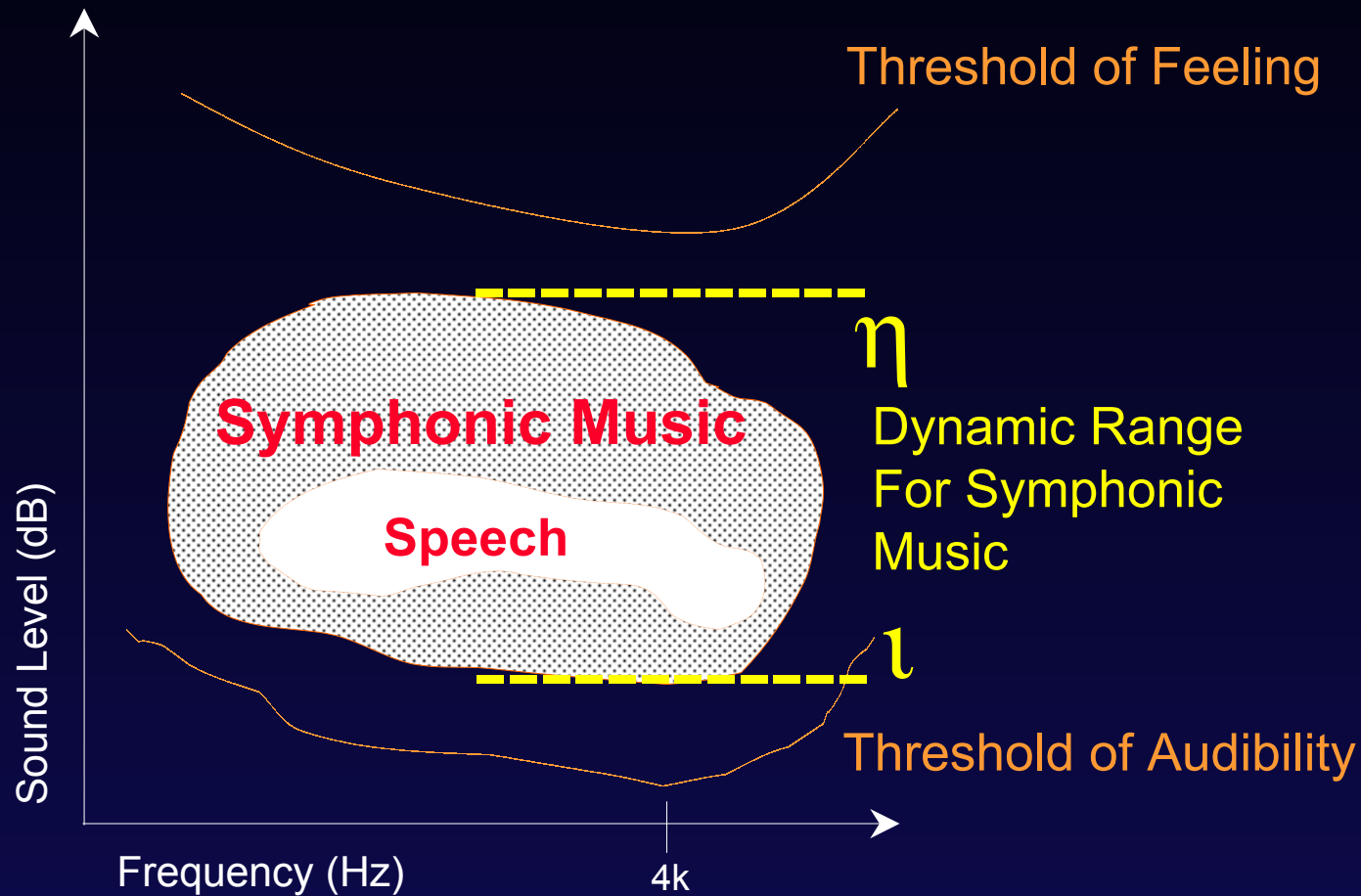


Figure 4

# Human Factors

Band	CTR. FREQ. (Hz)	Bandwidth (Hz)	Band	CTR. FREQ. (Hz)	Bandwidth (Hz)
1	50	100	13	1850	280
2	150	100	14	2150	320
3	250	100	15	2500	380
4	350	100	16	2900	450
5	450	110	17	3400	550
6	570	120	18	4000	700
7	700	140	19	4800	900
8	840	150	20	5800	1100
9	1000	160	21	7000	1300
10	1170	190	22	8500	1800
11	1370	210	23	10500	2500
12	1600	240	24	13500	3500

Figure 5

## Critical Bands

# Common Sounds

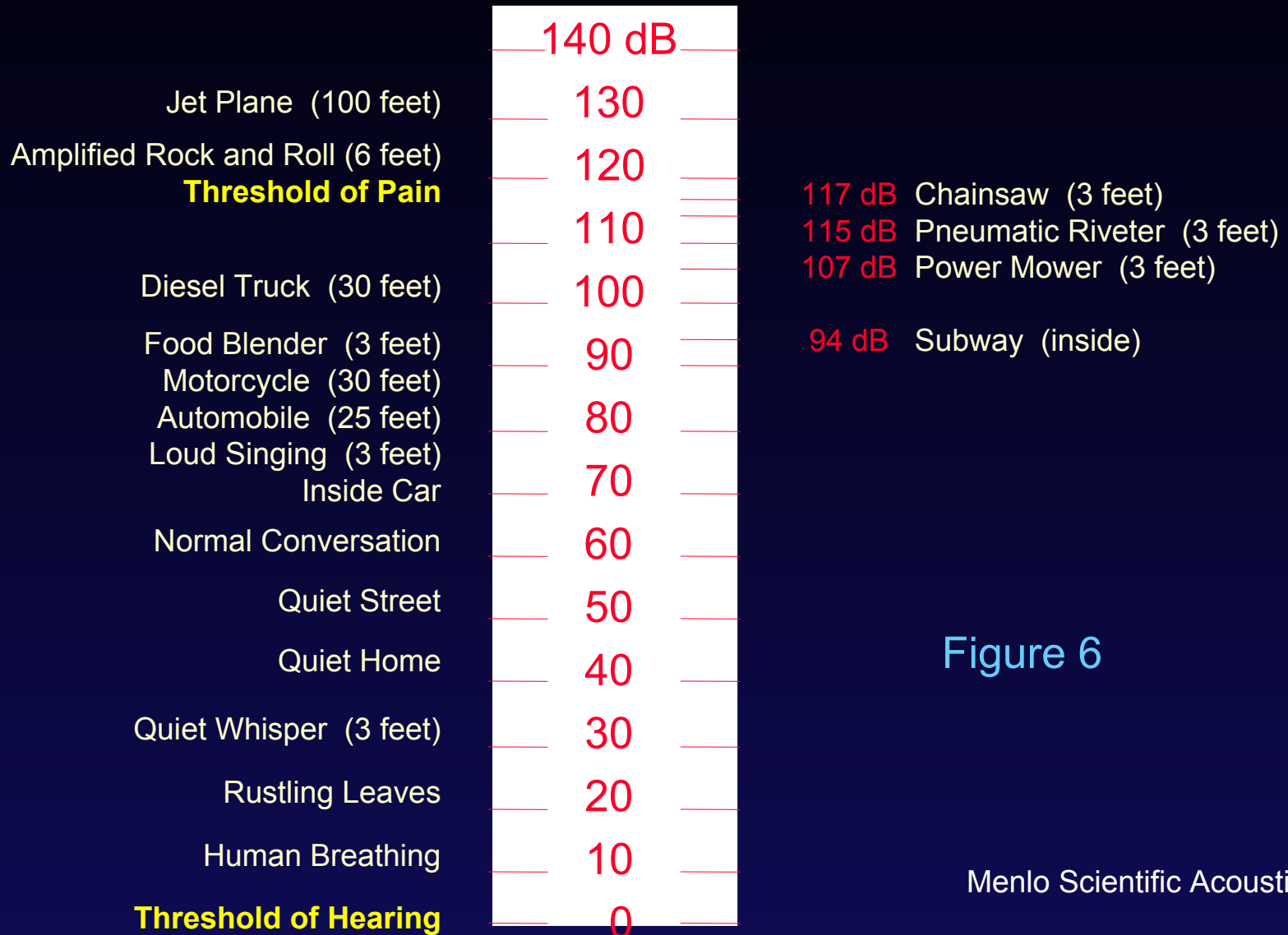


Figure 6

# Measurement

THIRD OCTAVE BAND NO.	CENTER FREQUENCY (Hz.)	FREQUENCY RANGE (Hz)	CORRESPONDING OCTAVE BAND
14	25	22 to 28	Sub-Octave 22 to 45
15	-- 31.5 --	28 to 36	
16	40	35 to 45	
17	50	45 to 56	1 45 to 89
18	-- 63 --	56 to 71	
19	80	71 to 89	
20	100	89 to 112	2 89 to 178
21	-- 125 --	112 to 141	
22	160	141 to 178	
23	200	178 to 224	3 178 to 355
24	-- 250 --	224 to 282	
25	315	282 to 355	
26	400	355 to 447	4 354 to 709
27	-- 500 --	447 to 563	
28	630	562 to 708	
29	800	708 to 892	5 707 to 1414
30	-- 1000 --	891 to 1123	
31	1250	1122 to 1413	
32	1600	1412 to 1779	6 1411 to 2822
33	-- 2000 --	1778 to 2240	
34	2500	2238 to 2819	
35	3150	2817 to 3549	7 2815 to 5630
36	-- 4000 --	3547 to 4469	
37	5000	4465 to 5625	
38	6300	5621 to 7082	8 5617 to 11234
39	-- 8000 --	7077 to 8916	
40	10000	8909 to 11225	

Figure 7



# History

## שמות תרומה כו

אָרְבַּע בָּאֵמָה הַרְיֵעָה הָאֶחָת מִדָּה אֶחָת לְכָל־הַיְרֵיעֹת:  
3 חֲמֵשׁ הַרְיֵיעֹת תִּהְיֶינָן הַבְּרִית אֲשֶׁה אֶל־אַחֲתָהּ וְחֲמֵשׁ יְרֵיעֹת  
4 הַבְּרִית אֲשֶׁה אֶל־אַחֲתָהּ: וְעִשִׂיתָ לְלֹאֵת תְּכַלֵּת עַל שֹׁפֵת  
הַרְיֵיעָה הָאֶחָת מִקְצֵה בַחֲבֵרֵת וּבֵן תַּעֲשֶׂההּ בַשֹּׁפֵת הַרְיֵיעָה  
הַתְּקוּצוּנָה בַּמִּחְבֵּרֵת הַשְּׁנִית: חֲמִשִּׁים לְלֹאֵת תַּעֲשֶׂההּ  
בַּיְרֵיעָה הָאֶחָת וְחֲמִשִּׁים לְלֹאֵת תַּעֲשֶׂההּ בַּקְצֵה הַרְיֵיעָה  
אֲשֶׁר בַּמִּחְבֵּרֵת הַשְּׁנִית מִקְבִּילֹת הַלְּלֹאֵת אֲשֶׁה אֶל־  
6 אַחֲתָהּ: וְעִשִׂיתָ חֲמִשִּׁים קָרְסֵי זָהָב וְחַבְרֹת אֶת־הַיְרֵיעֹת  
7 אֲשֶׁה אֶל־אַחֲתָהּ בַּקָּרְסִים וְהִנֵּה הַמִּשְׁכָּן אֶחָד: וְעִשִׂיתָ  
יְרֵיעֹת עוֹים לְאַהֲלֵי עַל־הַמִּשְׁכָּן עֶשְׂרֵ־עֶשְׂרֵה יְרֵיעֹת  
8 תַּעֲשֶׂה אֹתָם: אָרְדָּה הַרְיֵיעָה הָאֶחָת שְׁלֹשִׁים בָּאֵמָה  
וְרַחֵב אַרְבַּע בָּאֵמָה הַרְיֵיעָה הָאֶחָת מִדָּה אֶחָת לַעֲשִׂיתִי  
9 עֶשְׂרֵה יְרֵיעֹת: וְחַבְרֹת אֶת־חֲמֵשׁ הַרְיֵיעֹת לְבָד וְאֶת־  
שֵׁשׁ הַרְיֵיעֹת לְבָד וּבִפְלֹת אֶת־הַרְיֵיעָה הַשְּׁשִׁית אֶל־מִל  
י פָּנֵי הָאֹהֶל: וְעִשִׂיתָ חֲמִשִּׁים לְלֹאֵת עַל שֹׁפֵת הַרְיֵיעָה  
הָאֶחָת הַתְּקוּצוּנָה בַחֲבֵרֵת וְחֲמִשִּׁים לְלֹאֵת עַל שֹׁפֵת

v. 9 קמץ כו"ק

## שמות תרומה כה כו

33 וּשְׁלֹשָׁה קָנֵי מְנִיחָה מֵאֲדָה הַשְּׁנִי: שְׁלֹשָׁה גְבַעִים מִשְׁקָלֵים  
בַּקְנֵה הָאֶחָד כַּפְתָּר וּפְרָח וּשְׁלֹשָׁה גְבַעִים מִשְׁקָלֵים  
בַּקְנֵה הָאֶחָד כַּפְתָּר וּפְרָח בֵּן לַשֹּׁפֵת הַקָּנִים הַיְצִאִים  
34 מִן־הַמְּנִיחָה: וּבַמְנִיחָה אַרְבַּעַה גְבַעִים מִשְׁקָלֵים כַּפְתָּרִיהָ  
לָהּ וּפְרָחִיהָ: וּכַפְתָּר תַּחַת שְׁנֵי הַקָּנִים מִמֶּנָּה וּכַפְתָּר תַּחַת  
שְׁנֵי הַקָּנִים מִמֶּנָּה וּכַפְתָּר תַּחַת־שְׁנֵי הַקָּנִים מִמֶּנָּה לַשֹּׁפֵת  
36 הַקָּנִים הַיְצִאִים מִן־הַמְּנִיחָה: כַּפְתָּרִיהֶם וְקִנְתָּם מִמֶּנָּה  
37 יִהְיוּ כְּגֹה מִקְשֵׁה אֶחָת זָהָב טָהוֹר: וְעִשִׂיתָ אֶת־גִּרְתֵּיהֶן  
38 שְׁבָעָה וְהַעֲלֵה אֶת־גִּרְתֵּיהֶן וְהֵאָדָר עַל־עֹבֵר פְּנֵיהֶן: וּמִלְקַחֲתֶיהָ  
39 וּמִחֻתֹּתֶיהָ זָהָב טָהוֹר: כֶּכֶר זָהָב טָהוֹר יַעֲשֶׂה אֹתָהּ אֵת  
מ כָּל־הַכֹּהֲלִים הָאֵלֶּה: וְרָאָה וַעֲשֶׂה בְתַבְנִיתָם אֲשֶׁר־אַתָּה  
קָדָה כָּדָר: \* ם שליש

## כו CAP. XXVI

א וְאֶת־הַמִּשְׁכָּן תַּעֲשֶׂה עֶשְׂרֵה יְרֵיעֹת שֵׁשׁ מִשְׁנֹר וְתַכְלֵת  
וְאַרְגָּמָן וְתִלְעַת שְׁנֵי כַרְבִּים מַעֲשֶׂה חֹשֶׁב תַּעֲשֶׂה אֹתָם:  
2 אָרְדָּה הַרְיֵיעָה הָאֶחָת שְׁמֹנֶה וְעֶשְׂרִים בָּאֵמָה וְרַחֵב

כה' v. 39 סבירין תעשה

## Exodus XXVI

# History

## COLLECTED PAPERS ON ACOUSTICS

BY

WALLACE CLEMENT SABINE

LATE HOLLIS PROFESSOR OF MATHEMATICS AND NATURAL PHILOSOPHY  
IN HARVARD UNIVERSITY



CAMBRIDGE  
HARVARD UNIVERSITY PRESS  
1927

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# History

## ARCHITECTURAL ACOUSTICS

BY

VERN O. KNUDSEN, Ph.D.

*Professor of Physics and Dean of the Graduate Division  
University of California at Los Angeles*

NEW YORK

JOHN WILEY & SONS, Inc.

LONDON: CHAPMAN & HALL, LIMITED

# History

## ACOUSTICS

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LEO L. BERANEK

*Associate Professor of Communication Engineering  
Massachusetts Institute of Technology*

McGRAW-HILL BOOK COMPANY, INC.

New York Toronto London

1954

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# *History*



# Reflection

$$x > 4 \lambda$$

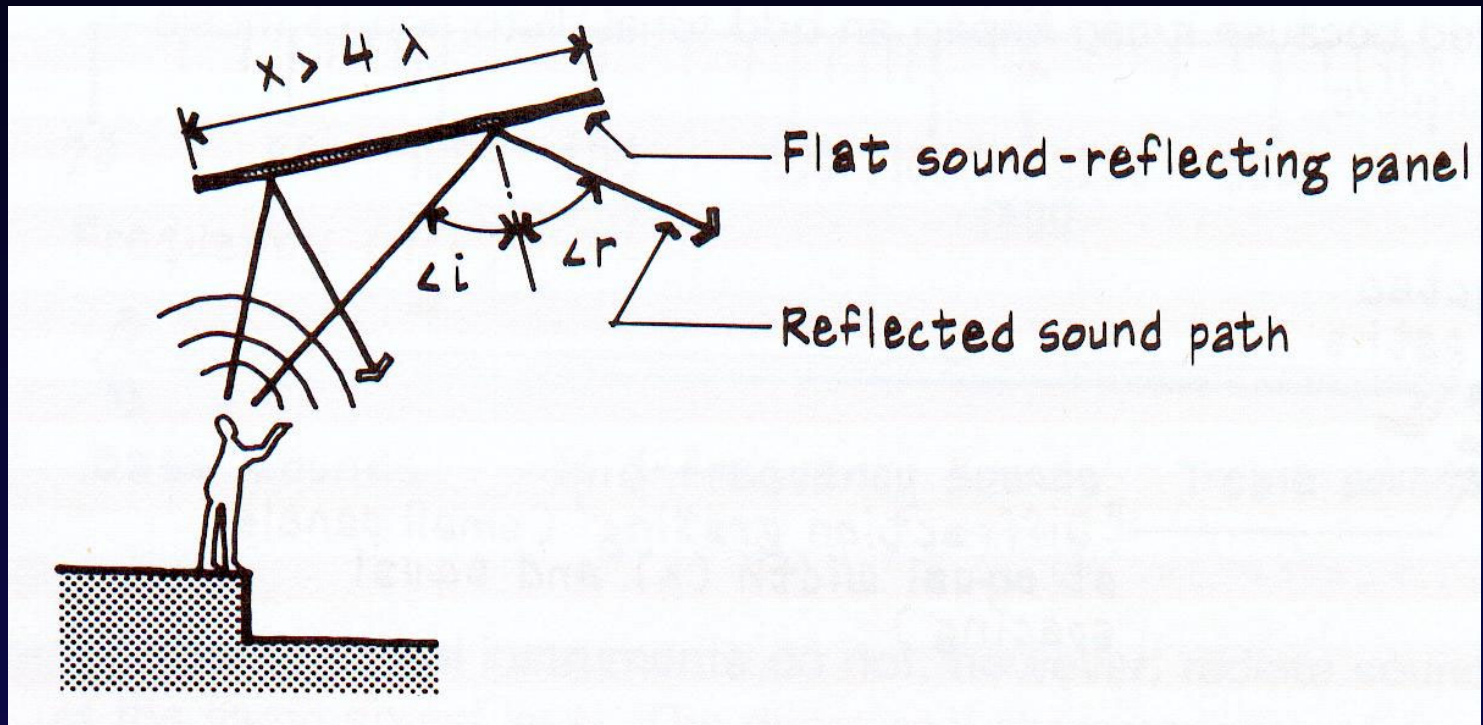


Figure 8

# Diffusion

$$x \approx \lambda$$

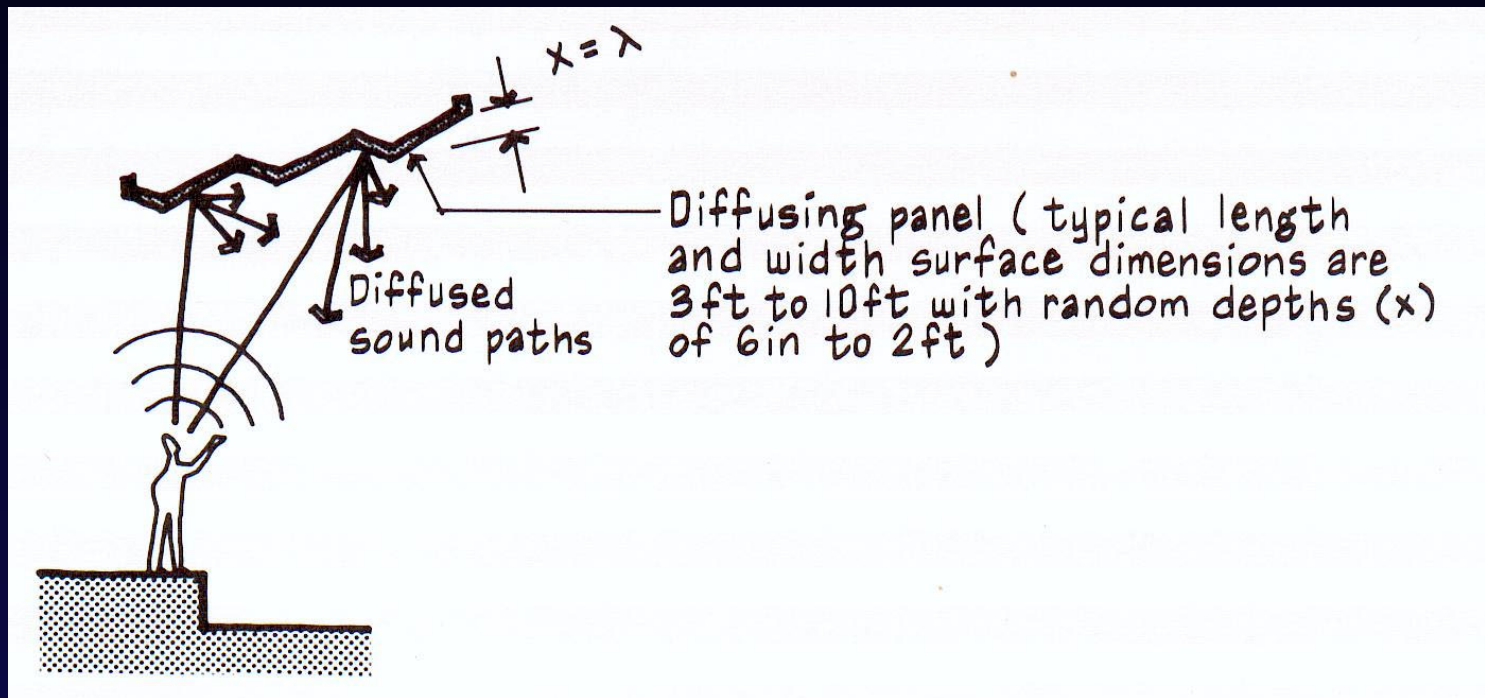


Figure 9

# Diffraction

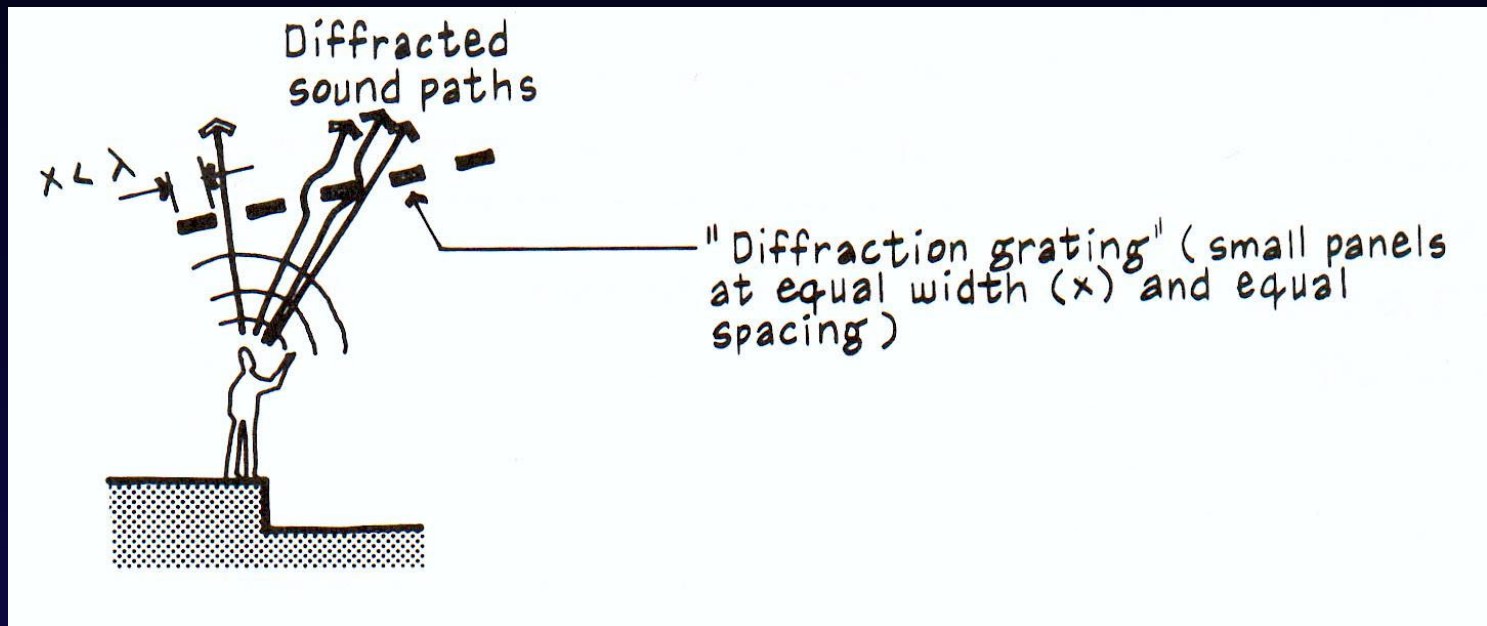


Figure 10



# Concave Reflector

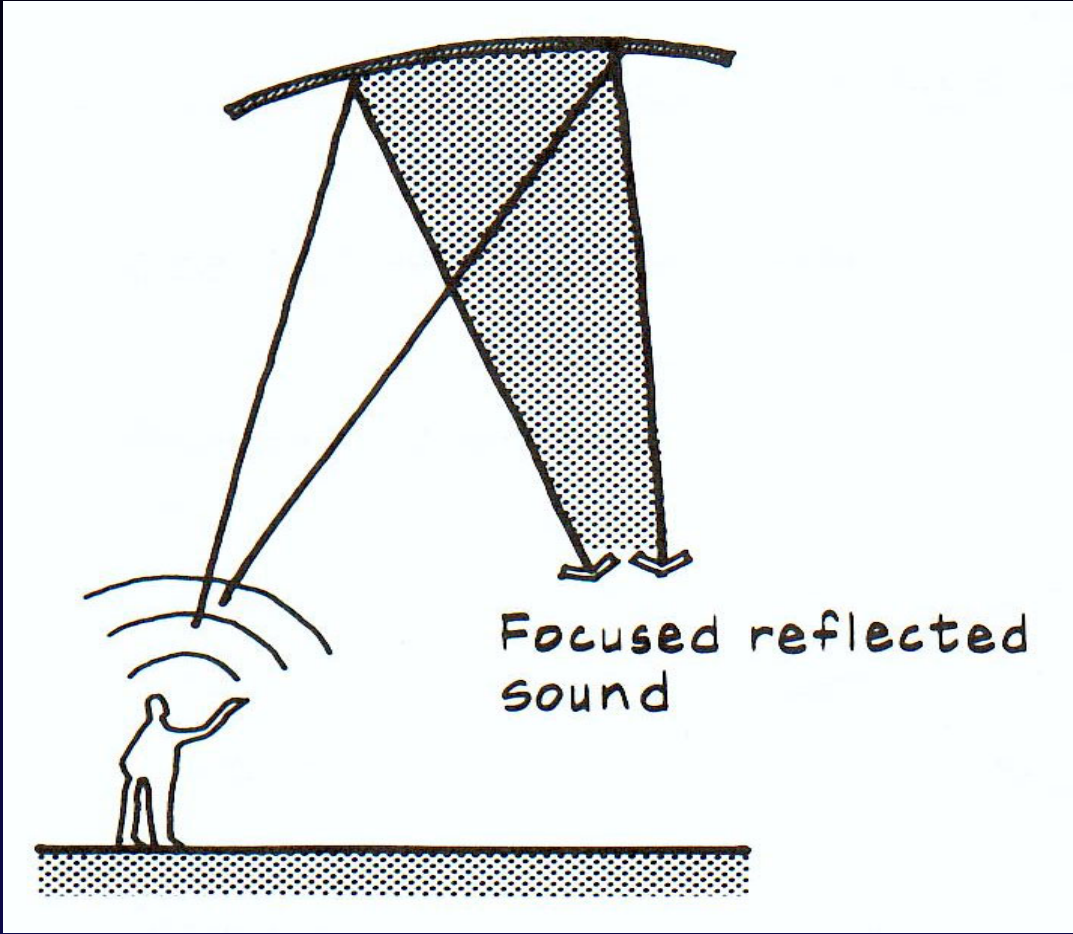


Figure 11

# Flat Reflector

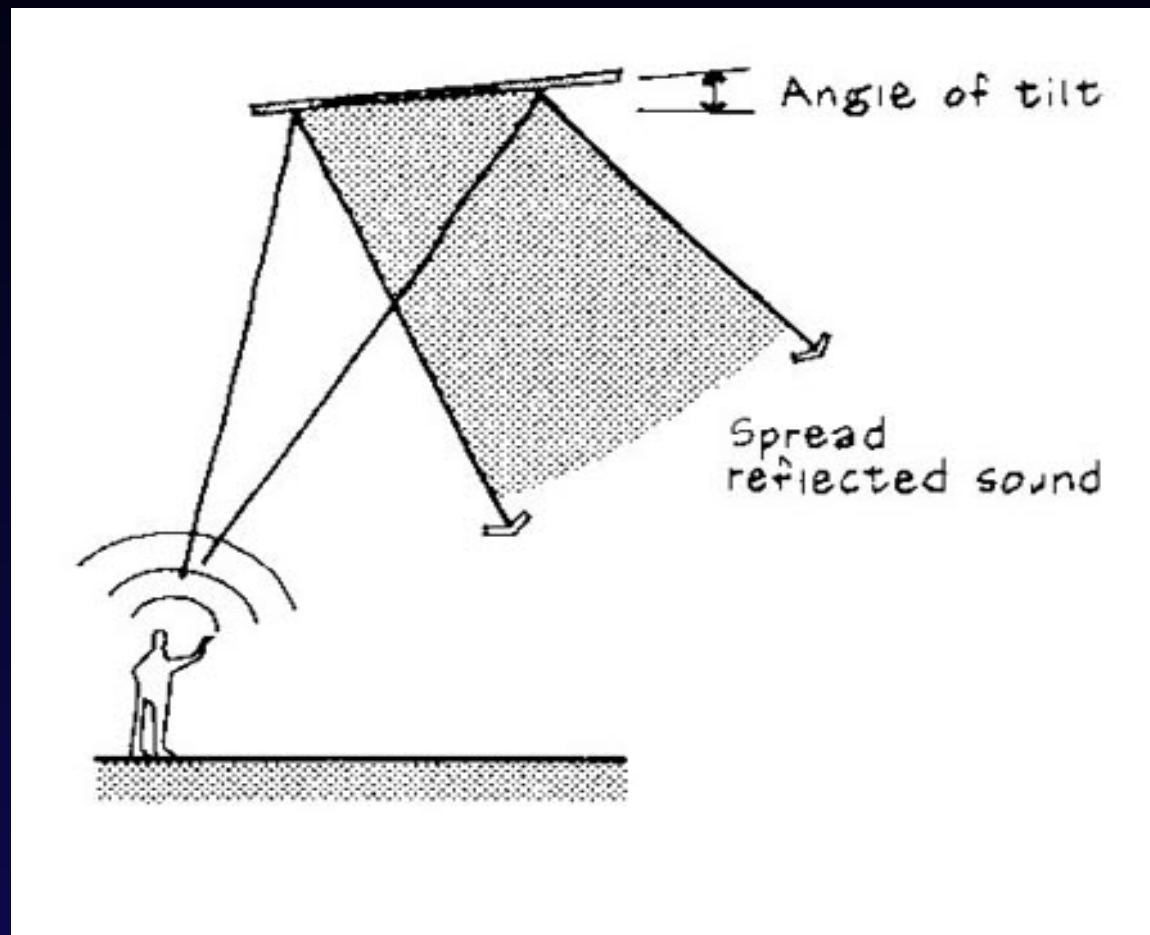


Figure 12

# Convex Reflector

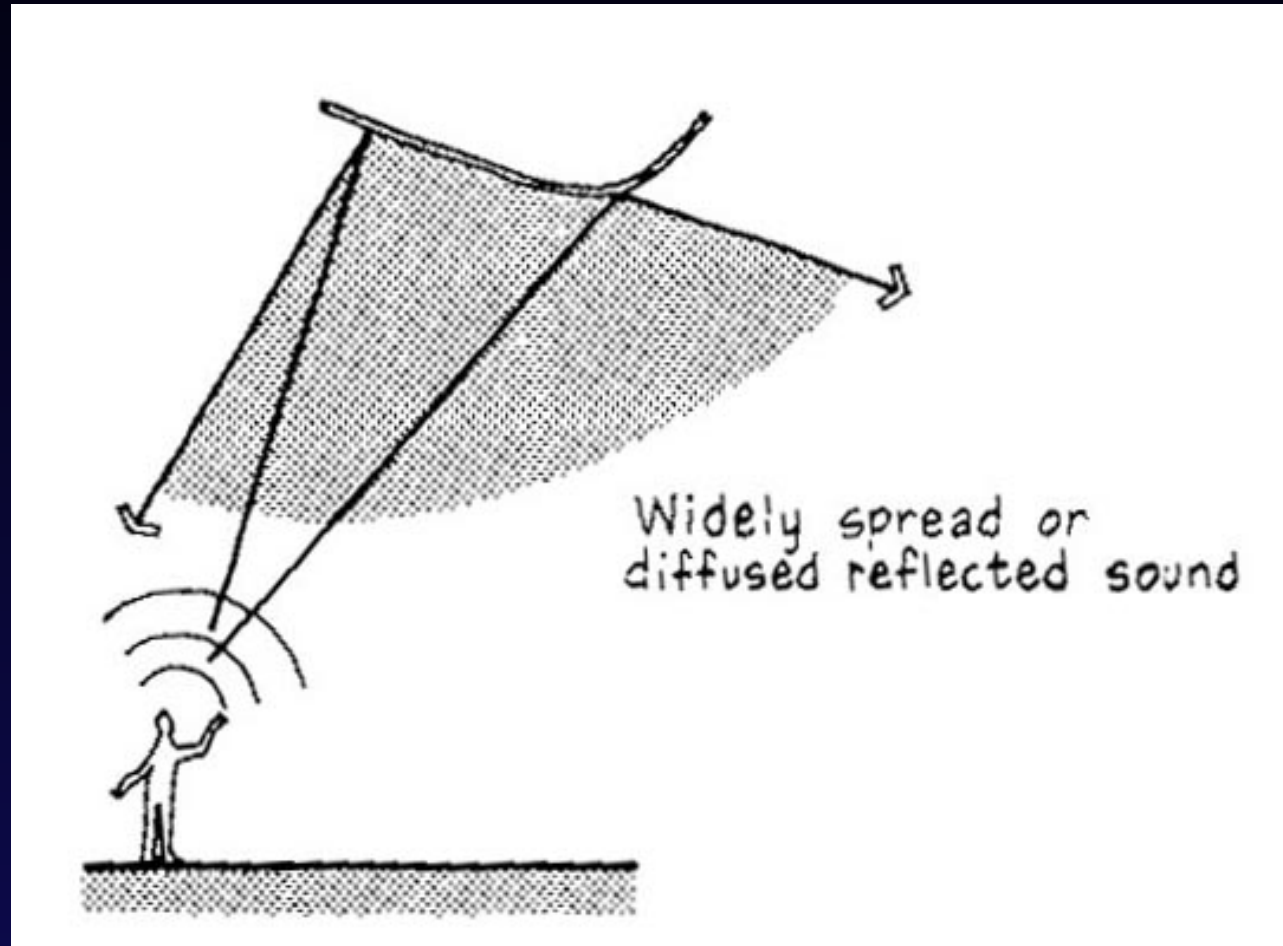


Figure 13

# Room Modes

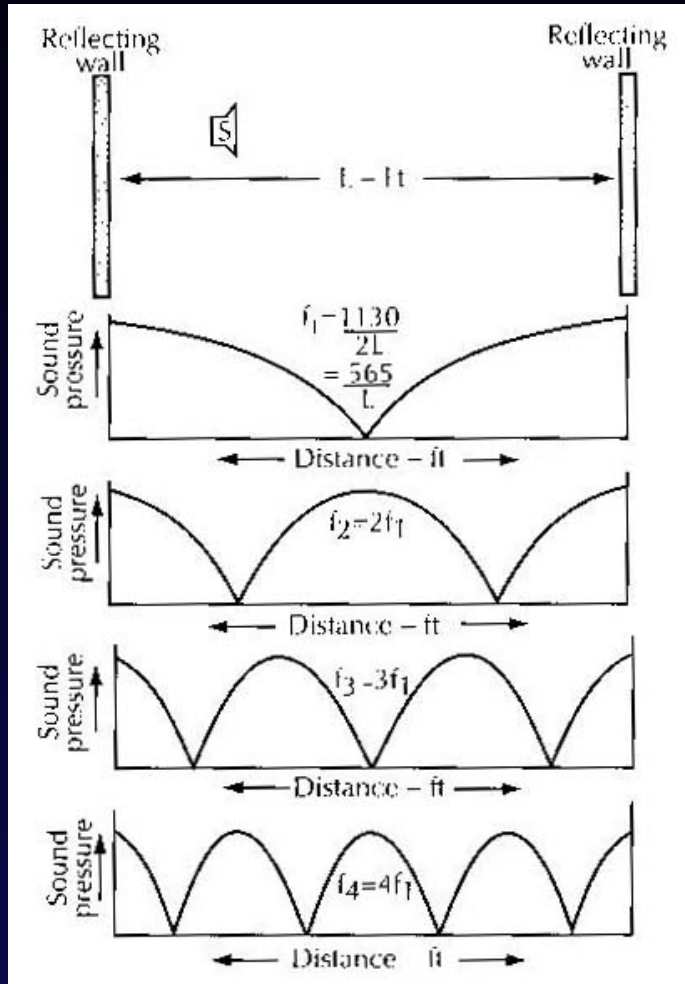


Figure 14

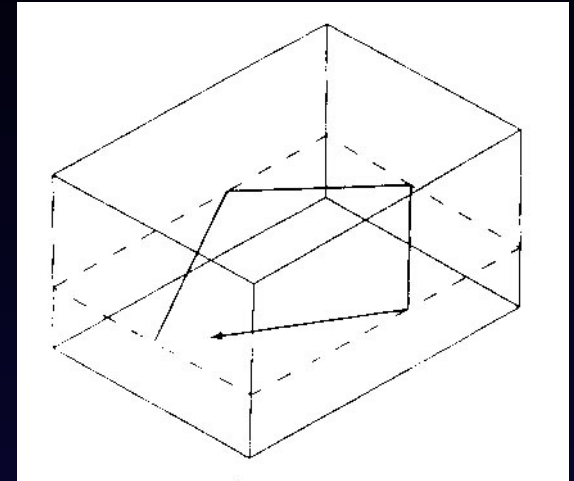


Figure 15

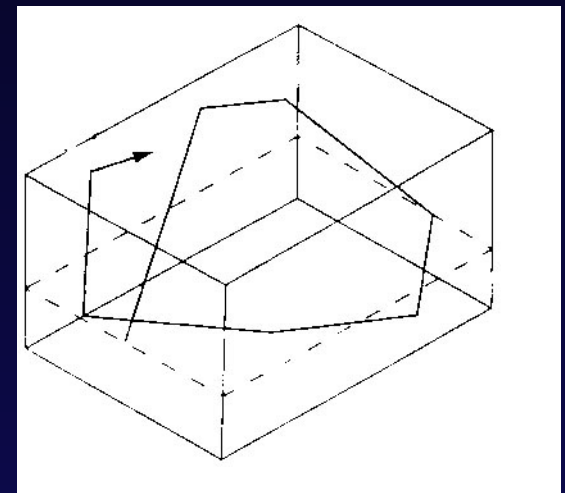


Figure 16

# Reverberant Decay

## large room

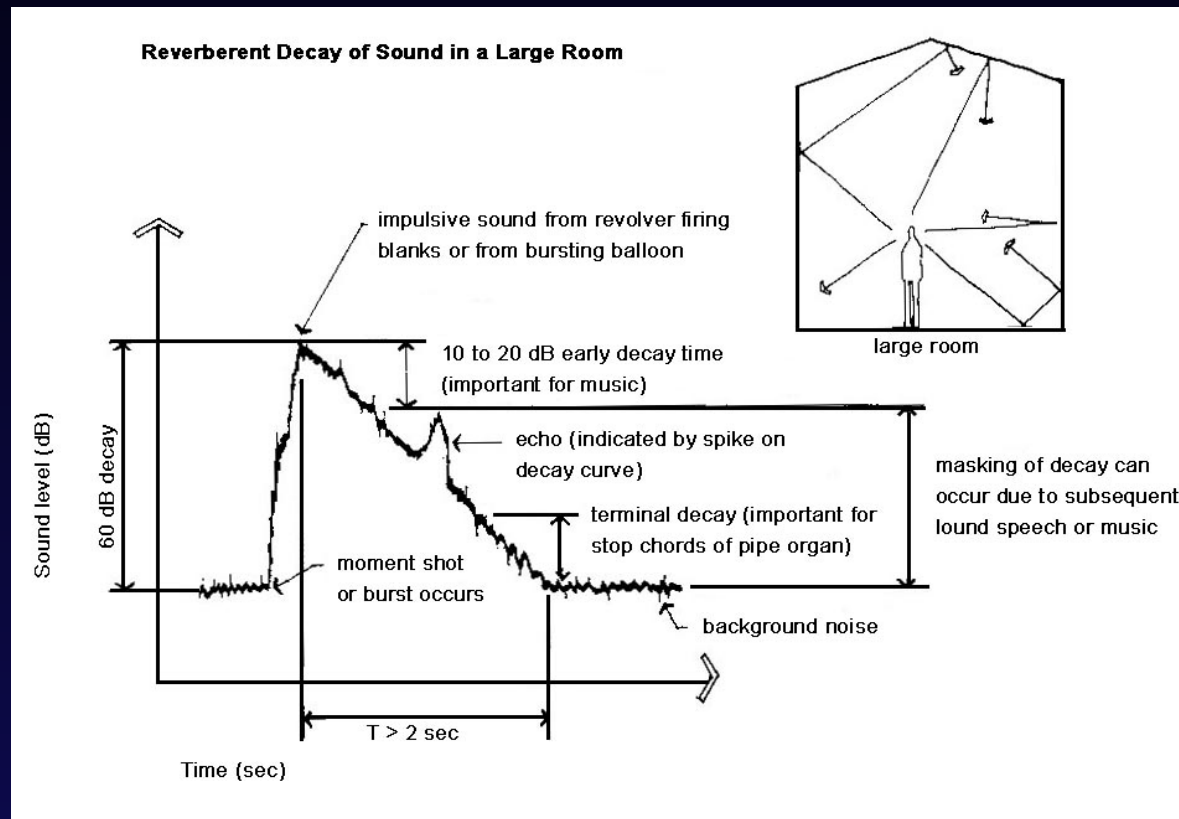


Figure 17

# Reverberant Decay

## small room

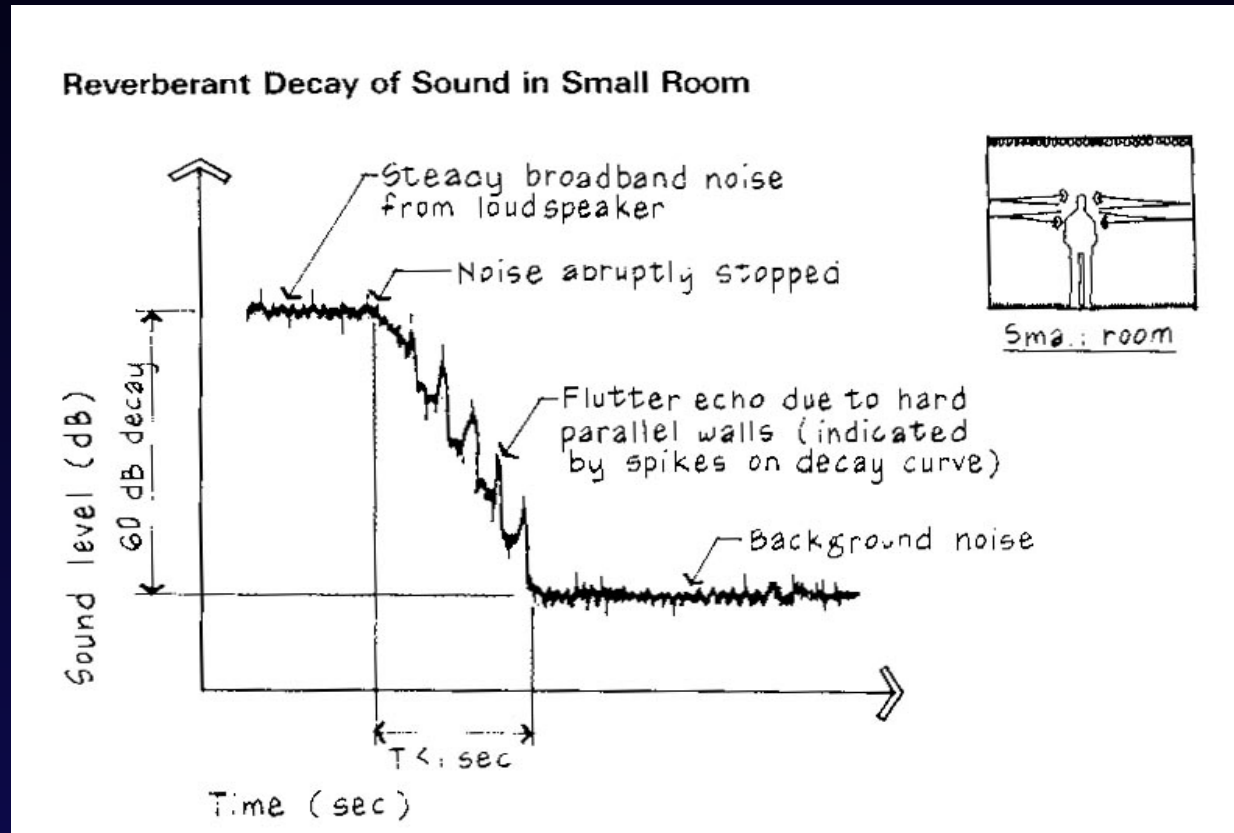


Figure 18

# Materials

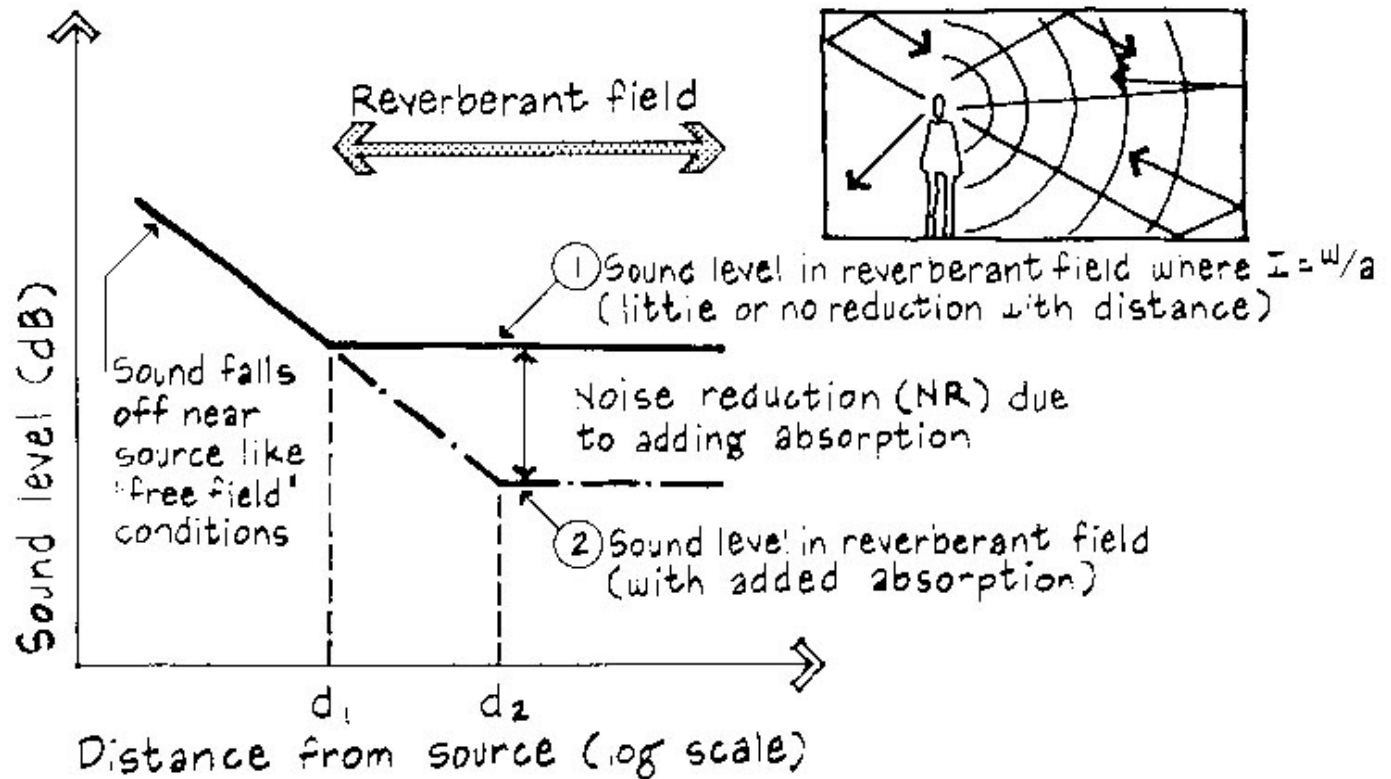


Figure 19

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# *Small Rooms*

- Modes
- Shape
- Reflection management



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# *Large Rooms*

## TIME METRICS

Reverberation Time (*RT60*)

Bass Ratio (*BR*)

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# Large Rooms

## ENERGY METRICS

Strength ( $G$ )

Speech Time Index ( $STI$ )

Sound Pressure Distribution ( $\Delta L$ )

Articulation Loss ( $AL_{cons}$ )

Center Time ( $t_s$ )

Subjective Intelligibility Tests

Energy Definition Measure ( $C_{50}$ )

Clarity ( $C_{80}$ )

Register Balance Measure ( $B_R$ )

Sound Coloration ( $K_t$  and  $K_h$ )

---

# Large Rooms

Spacial Impression Measure  
for Music ( $R$ )

Lateral Efficiency  
( $LE$  for Music,  $LF$  and  $LFC$ )

Interaural Cross Correlation  
Coefficient ( $IACC$ )

Interaural Time-Delay Gap  
( $ITDG$ ,  $t_1$ )

Reverberance Measure ( $H$ )

Diffusion

Stage Support ( $ST1$ )

Texture

Early Decay Time ( $EDT$ )

Intimacy

Spaciousness

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# References

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# List of Figures

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- Figure 4: derived from Egan, p 9
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